

EFR summary

Finance 1, FEB12003X

2025 - 2026



Lectures and Exercise Lectures 1 to 6
Weeks 1 to 6

Deloitte.

DeNederlandscheBank

EUROSYSTEEM

Details

Subject: Finance 1 IBEB 2025 - 2026

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Date of publication: 13.02.2026

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Finance 1 – IBEB – Lecture 1, week 1

Finance overview

Price is what you pay today while value is what you receive in the future, and the difference of the 2 determines your return

- The future value is uncertain, meaning there is risk, where the higher the risk a higher expected return is required

Conceptual pillars in Finance

1. Financial markets connect savers and firms (investors)

- It moves money to most efficient projects
- Connect people with money to people who need money (nowadays through platform)
- Markets are powerful often very efficient, where price reflect knowledge of millions of investors (at that moment) and helps companies grow and create jobs

2. Capital is allocated based on risk and expected return (Investment decisions)

- How do companies decide which projects to invest in, finance tries to solve this using
 - o The trade-off between risk and return
 - o Time value of money: Trade-offs across time
 - o Financing choices: own funds, equity or debt

3. Markets allow risk sharing and diversification

- Spreading risk by owning shares of different companies instead of only one helps reduce risk, thus lowering cost of investing and more projects become viable
- At the household level, diversification helps save and invest for the long run

4. Financial institutions are the intermediate between savers and firms (investors)

- In the real-world funding from shareholders to firms is not direct, there are intermediaries: Banks, Private equity, Other financial institutions
- Regulation and oversight is a must to enforce rules

Types of financial statements

Balance Sheet. Firm's financial position at a point in time (firm's assets and liabilities)

Income Statement. Firm's earnings (firm's revenues and expenses)

Statement of Cash Flows. Indicates the amount of cash generated by the firm.

Statement of Stockholders' Equity. Breaks down the stockholders' equity into issuing shares and retained earnings.

Statement of cash flows

Usually, **Net income** is not equal to the amount of cash the firm has earned due to:

- Non-cash expenses (e.g. Depreciation & Amortization) which are taken into account in the net income, but you do not actual pay cash for it
- Uses of cash not on the income statement (e.g. Investment in PPE), meaning decrease in actual cash earned
 - o Capital Expenditure
 - o Change in (Current assets – Current liabilities)

Free cash flow (FCF) – the cash flow available for the company to repay creditors, pay dividends and interest to investors.

- The statement of cash flow includes **3 sections:** Operating activity, investing activity, and financing activity

Factor	Location
+ EBIT x (1- Tax Rate)	Income Statement
+ Non-cash Expenses (Depreciation, Amortization, etc.)	Income Statement
- Change in (Current Assets - Current Liabilities)	Balance Sheet (current period and previous period)
- Capital Expenditures (CAPEX)	Balance Sheet: Property, Plant, and Equipment (current period and previous period)
= Free Cash Flow	

Valuation indicators

Book value versus market value

Book value: how accountants evaluate a firm based on the sum of the net profits that were not paid out as dividends over the lifetime of the company. This is the book value of the firm's equity (Equity = Assets - Liability).

Financial economists, on the other hand, assess the value of a firm's equity by looking at its **market value** (or market capitalisation). This equals # shares outstanding * stock price.

$$\text{market-to-book (MB) ratio} = \text{market value of equity} / \text{book value of equity}$$

When creditors and shareholders have more positive views on the firm's future than the suggestion from its book value, MB is often greater than 1. An obvious example is the potentially huge difference between the market value and the book value of a (great) football player.

Enterprise value: the market value of the firm's (underlying) assets that generate cash flows. This is the cost one needs to pay when taking over the enterprise.

$$\text{enterprise value (EV)} = \text{market value of equity} + \text{debt} - \text{cash.}$$

Cash here is the excess cash that is not needed for the firm's operating activities and can be paid back to investors without harming the business. This is different from working capital (cash needed to run the firm).

Fundamentals in Finance

Risk-return relations

Risk is the chance that the outcome is different than expected (care more about losses)

- The higher the risk, the higher the required return.

E.g. You can invest in 2 projects, investing \$ 950 today gives you

1. \$1000 in 2 years with 100% certainty
2. \$ 2000 in 2 years with 50% probability or \$ 0 with 50%

Both have the same expected outcome. But one guarantees (profit of 50) and the other is uncertain (profit of 1050 or loss of 950)

- Project 2 is riskier, and generally investors are risk-averse (don't like risk)

No arbitrage

Arbitrage: without taking risks, you make a profit

No arbitrage: you cannot make a profit without taking risks

E.g. You can buy McDonalds chicken meal for a total of \$ 4.99, and then sell the different item individually, fries, coke and nuggets, this gives you a total of \$ 6.01.

- Meaning a profit of $\$6.01 - \$4.99 = \$1.02$

This is arbitrage profits, however there are limits to Arbitrage

- May not exist for long:
- Transaction costs
- Hidden risks
- Opportunity costs

Due to the limitations above we have the No-arbitrage principle, where risk free profit opportunities cannot persist, this implies the following

- If 2 assets deliver the same cash flows in all states, they must have the same price, '**Law of one price**'
- Intuitively, if prices differed investors could buy the cheaper asset and sell the more expensive one, trades like this with time will eliminate the price difference
- This analogy forms the foundation for pricing, valuation, and relative comparison of assets

Law of one price: If equivalent investment opportunities trade simultaneously in different markets, then the price of trading should be the same everywhere. If this law does not hold, then an arbitrage opportunity exists.

Finance 1 – IBEB

Exercise lecture 1, week 1

Introduction to financial statement analysis

Firms' disclosure of financial information

Financial statements are firm-issued accounting reports with past performance information. They are filled with the SEC (Securities and Exchange Commission). Financial statement analysis is used to compare the firm with itself over time, and compare the firm to other similar firms.

Balance sheet

A firm's balance sheet is a snapshot in time of the firm's financial position.

The balance sheet identity is given by:

$$\text{Assets} = \text{Liabilities} + \text{Stockholders' Equity}.$$

Assets: what the firm owns.

- **Current assets:** cash or assets that are expected to be turned into cash within a year. This category includes cash, marketable securities (short-term low-risk investments like government bonds), accounts receivable, inventories, and other current assets such as pre-paid expenses.
- **Long-term assets** include net property, plant, and equipment (book value=cost of acquisition-accumulated depreciation), goodwill and intangible assets and other long-term assets, such as investments in long-term securities.

Liabilities: what the firm owes.

- **Current liabilities** are to be paid within a year. This includes accounts payable, short-term debt/notes payable, current maturities of long-term debt, and other current liabilities such as taxes payable, wages payable.

Net working capital is the capital that is available in the short term to run the business:

$$\text{Net working capital} = \text{current assets} - \text{current liabilities}.$$

- **Long-term liabilities** consist of other liabilities with the maturity of longer than one year and include long-term debt, capital leases, and deferred taxes.

Stockholders' Equity: the difference between the value of the firm's assets and liabilities.

- **Book value of equity** can be negative because it is calculated as the difference between book value of assets and book value of liabilities. However, many of the firm's valuable assets may not be reflected in the balance sheet (for example: the firm's reputation).
- **Market value of equity** (Market Capitalization) = Market price per share × number of shares outstanding. This cannot be negative and often differs substantially from book value.
- **Market-to-book ratio** (or Price-to-book ratio)

$$\text{market-to-book (MB) ratio} = \text{market value of equity} / \text{book value of equity}$$
 Value stocks: $MB \text{ ratio} < 1$
 Growth stocks: $MB \text{ ratio} > 1$
- **Total enterprise value** (TEV)

$$\text{enterprise value (EV)} = \text{market value of equity} + \text{debt} - \text{cash}$$

Income statement

Income statement indicates the flows of revenues and expenses over a period of time.

- An important component of an income statement is the "bottom line" (net income = earnings in a period).

Earning calculations:

Total sales/revenue

-

Cost of sales

Gross profit

-

Operating expenses

 Operating income
 +/-
 Other income/expenses

 Earnings before interest and tax (EBIT)
 +/-
 Interest income/interest expenses

 Pre tax income
 -
 Taxes

 Net income

Net income/N° of shares outstanding = EPS

Statement of Cash Flows

Net income typically does not equal the amount of cash the firm has earned, because it includes non-cash expenses such as depreciation and amortization, and excludes cash uses such as investment in property, plant, and equipment or expenditure on inventory.

A statement of cash flows can be used to calculate free cash flows (FCF) and enterprise value. It includes three sections:

1. Operating Activity: Adjusts net income for all non-cash items related to operating activities and changes in net working capital.

Adjustments:

- Depreciation / amortization: add the amount of depreciation / amortization (as a non-cash expense)
- Account receivable: deduct the increases (as the cash is not yet been received)
- Accounts payable: add the increases (cash have not been paid yet)
- Inventories: deduct the increases (any increases in inventory are paid by cash)

2. Investment Activity: all cash required for investment activities

- Capital expenditures (purchasing PPE)

- Trading of marketable securities
- Acquisition related expenditures

3. Financing Activity:

- Payments of dividends (cash outflow, therefore is deducted)
retained earnings = net income - dividends
- Changes in borrowings (increases in borrowings are cash inflows)

Financial statements analysis & ratios

These financial statements are used to:

- Compare the firm to itself over time
- Compare the firm to other similar firms

We can derive different financial ratios from these statements to assess different factors of the firm

- **Profitability ratios:** e.g. Gross margin ratio
- **Liquidity ratios:** e.g. Current ratio
- **Working capital ratios:** e.g. Account receivable/payable days
- **Interest coverage and leverage ratios:** e.g. EBIT interest coverage ratio, debt-to-enterprise value ratio
- **Valuation ratios:** e.g. Enterprise value to EBITDA

Financial decision-making and law of one price

Decision rules based on benefits and costs need to be made at the same moment in time

- When we express the value in terms of dollars today, we call it the **present value (PV)** of the investment
- When we express the value in terms of dollars in the future, we call it the **future value (FV)** of the investment

Financial decision making: Investment should be made when $PV(\text{benefits}) > PV(\text{costs})$.

$$NPV = PV(\text{benefits}) - PV(\text{costs}) \rightarrow NPV > 0$$

Arbitrage refers to taking advantage of the price difference when buying and selling equivalent goods in different markets. An arbitrage opportunity occurs

when it is possible to make a profit without taking any risk or making any investment.

Normal market is a competitive market in which there is no arbitrage opportunity.

Law of One Price: If equivalent investment opportunities are traded at the same time in different normal markets, then they must trade for the same price in both markets.

Finance 1 – IBEB Lecture 2, week 2

Time value of money

Financial decisions are often made by comparing values:

1. Values can be compared only at the same point in time
2. Compound cash flow to move it forward in time

$$FV_n = C * (1 + r)^n$$

3. Discount cash flow to move it backward in time:

$$PV = \frac{C}{(1 + r)^n}$$

Valuing a stream of cash flows

Present value of a cash flow stream

$$PV = \sum_{n=0}^N \frac{C_n}{(1 + r)^n}$$

Future value of a cash flow stream

$$FV = PV(1 + r)^n$$

Annuities - Fixed period.

- Constant cash Flow or cash flow with constant growth

$$PV(\text{annuity with growth}) = \frac{C}{(r + g)} \left[1 - \left(\frac{1 + g}{1 + r} \right)^N \right]$$

Perpetuities - Infinite life.

- Constant cash Flow or cash flow with constant growth

$$PV(\text{perpetuity}) = C/r$$
$$PV(\text{growing perpetuity}) = C/(r - g)$$

Note: Infinite life, but not infinite value if $g < r$, usually this is the case

- Both Annuities and Perpetuities start 1 year from today, so if the question specify that it starts, say 2 years from today then you must discount it once more

$$\frac{1}{1 + r} \cdot \frac{C}{r}$$

Discounting with the risk-free rate

Risk-free interest rate, r_f : interest rate at which money can be borrowed or lent without risk over that period

If future payments are risky, premium needs to be added to interest rate to account for riskiness (higher risk => higher interest rate).

Financial decision-making with NPV

Cost-benefit analysis for an investment opportunity can be done by calculating the Net Present Value (NPV) using the formula:

$$NPV = PV(benefits) - PV(costs)$$

NPV decision rule: invest in the alternative with the highest NPV. Choosing this alternative is equivalent to receiving its NPV in cash today.

The net present value of a stream of cash flows can be valued by summing the discounted values of each future cash flow with the appropriate interest rates regarding the time distance.

E.g. you give me EUR 100 now. After one year, I'll give you EUR 107. r_f is 5%

- $NPV = 107 / (1+5\%) - 100 = 101.90 - 100 = 1.90$
- This is a good deal as NPV is positive. This reflects that the 107 is more than the 105 that you'd invest the 100 on a bank account

Valuing bonds

Bonds cashflows amount and timing tend to be known in advance (they are **fixed**)

- It's a security issued by a borrower (e.g. government or company) and purchased by an investor.
- The bond issuer is raising money (borrowing) today
- The investor has delivered some money to the issuer (a loan) and expects to see regular cashflows repaying this money over time

Cash flows:

- Investor pays the bond Price
- Issuer pays the pre-specified payments: Coupons and final repayment

Note: We need to use present value techniques to compare cash flows

Two types of bonds

1. Zero coupon bond: Offers a single payment.

- Purchaser pays the price of the bond
- The bond promises in K-year to pay the bondholder a single payment, called **face value** (par value)
- The date of this payment is called the **maturity date**. K is the time to maturity

2. Coupon bond: Zero coupon bonds with additional periodic payments

- The bond promises in K-year to pay the bondholder a single payment, called face value
- The date of this payment is called the maturity date. K is the time to maturity
- Additional coupons: At regular intervals until maturity, the bondholder receives a coupon payment
- Coupon rate: the ratio of total annual coupon to face value

Bond price: present value of cash flows

Step 1: Identify all cash flows

Step 2: Discount these cash flows using rules of time travel. For very long-term bonds, we can use the annuity formula for the coupons + present value of final payment of face value

- Annuity without growth

$$PV_A = \frac{C}{r} \left[1 - \left(\frac{1}{1+r} \right)^T \right]$$

- Bond value = PV (coupon value) + PV (face value)

$$PV_B = \frac{Coupon}{r} \left[1 - \left(\frac{1}{1+r} \right)^T \right] + \frac{Face\ value}{(1+r)^T}$$

Examples

The following tables show the Cash flow of the following bonds

- Five-year coupon bond with face value of 1000, coupon rate and interest rate 5%
- Five-year zero-coupon bond with face value of 1000, interest rate is 5%
- Reversed question: If the price is 1000 of a zero-coupon bond with a 5-year maturity
 - What is the face value?

	CF Coupon	CF Face value	PV	CF	PV	CF	PV
today			1000.00		783.53		1000.00
t = 1	50		47.62		0.00		0.00
t = 2	50		45.35		0.00		0.00
t = 3	50		43.19		0.00		0.00
t = 4	50		41.14		0.00		0.00
t = 5	50	1000	822.70	1000	783.53	1276.28	1000.00

What drives bond prices

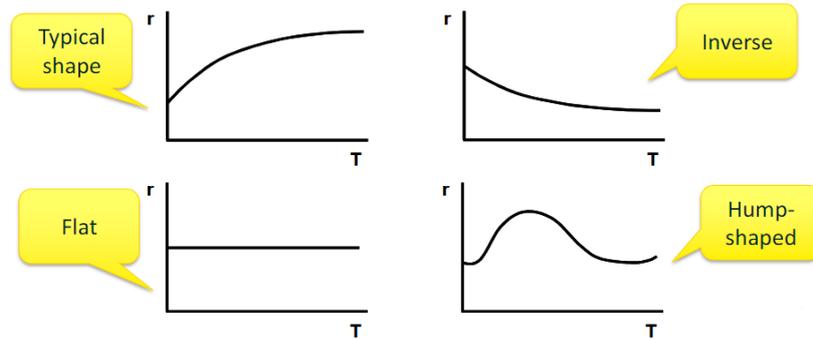
1. Interest rate

If after the issue of a bond, the general level of discount rates in the economy rose then we would expect bond prices to fall.

- When a bond is issued the coupon rate should reflect the current market conditions (interest rates)
- **Note:** cashflow to be received at different future dates should be discounted using different discount rates
 - We call these the #-year spot rates

Term structure of interest rates indicates how interest rates vary with the maturity at one point in time.

- The most typical case depicts an upward-sloping term structure, because the longer the time until maturity the higher the interest rate.
- But there can also be different variations



2. Risk of default

The possibility of default adds a credit spread, increasing the required return and lowering the bond's price.

Credit spread is a risk premium, that compensates for taking risk

$$Price = \sum_{t=1}^T \frac{Face\ value}{(1 + r_f + credit\ spread)^t}$$

Bond price: yield to maturity

We often use Yield to Maturity rather than the bond price because,

- Bond prices may differ because of coupon rates
- YTM is an annual rate and much more comparable

Yield to Maturity is the constant, hypothetical discount rate that equates the PV of the bonds cashflow with it's price

- Basically, we solve for the YTM and get a fixed rate

High bond price must mean a low YTM and low price means high YTM

$$Price = \frac{C_1}{(1 + YTM)} + \frac{C_2}{(1 + YTM)^2} + \dots + \frac{C_n}{(1 + YTM)^n} + \frac{Face\ value_n}{(1 + YTM)^n}$$

If we know the price, we can calculate the yield (and vice versa)

YTM is the weighted average of all spot rate used for discounting, this because different spot rates are discounted more or less, depending on the year

$$Price = \sum_{t=1}^T \frac{C_t}{(1 + r_t)^t} = \sum_{t=1}^T \frac{C_t}{(1 + YTM)^t}$$

Finance 1 – Exercise lecture 2, week 2

Time value of money

It is not possible to simply sum or subtract cash flows that occur at different points in time, this is because of time value of money, as we have seen last week, we have to express all cash flows at the **same point in time**

- Moving cash flow backward, by expressing all future cash flows' values by **discounting** them to today
- Moving cash flow forward, by expressing all cash flows at a period later than today by **compounding** them

So, to calculate the PV of a stream of cash flows you should discount them to today, but if you have many cash flows this can take quite some time

- For this we have 4 short-cut formulas

PV shortcut formulas

g = growth rate, n = number of periods, c = cash flow, r = interest rate

Type of cash flows	Constant cash flows	Growing cash flows
Perpetuities (last forever)	$g = 0, n \rightarrow \infty$ $PV(\text{perpetuity}) = \frac{C}{r}$	$g < r, n \rightarrow \infty$ $PV(\text{growing perpetuity}) = \frac{C}{(r-g)}$
Annuities (N periods)	$g = 0, n \rightarrow N$ $PV(\text{annuity}) = \frac{C}{r} \times \left[1 - \frac{1}{(1+r)^N} \right]$	$n \rightarrow N$ $PV(\text{growing annuity}) = \frac{C}{r-g} \times \left[1 - \left(\frac{1+g}{1+r} \right)^N \right]$

Note: If you know the formula for growing annuities you know them all

Interest rates

Effective Annual Rate (EAR) indicates the total amount of interest that will be earned at the end of one year.

- Typically used in present value calculations for yearly cash flows as it considers the effect of compounding.
- Also referred to as the Effective Annual Yield (EAY) or Annual Percentage Yield (APY).

Annual Percentage Rate (APR) indicates the amount of simple interest earned in one year.

- **Simple interest** is the amount of interest earned without the effect of compounding.
- The APR is typically less than the EAR.

Note that the APR cannot be used as a discount rate without adjustments made.

The APR with k compounding periods is a way of quoting the actual interest earned each compounding period:

$$\text{Interest Rate per Compounding Period} = APR / \left(\frac{k \text{ periods}}{\text{year}} \right)$$

To convert an APR to an EAR, we can use the following formula:

$$1 + EAR = \left(1 + \frac{APR}{k} \right)^k$$

- The EAR increases with the frequency of compounding, where **continuous compounding** is compounding every instant

Valuing bonds

Bond: A tradable loan, which generally has a fixed maturity and fixed coupon payments (cash flow stream).

Two types of bonds

We have Coupon bond and Zero-coupon bonds, the main difference is that one only pays out a **face value**, but the other has additional **coupon payments**, this is explained more precisely on Lecture 2 of week 2

Yield to maturity: The discount rate that sets the present value of the promised bond payment equal to the current market price of the bond

Relation between spot rate and forward rates

An **interest rate forward contract** or **forward rate agreement** is a contract today that fixes the interest rate for a loan or investment in the future.

Suppose we have the following options:

- Invest in a risk-free 2 year 0-coupon bond
- Invest in a risk-free 1 year 0-coupon bond and a 1 year forward contract for the second period

By the law of one price these 2 must have the same return

$$(1 + r_2)^2 = (1 + r_1)(1 + f_2)$$

- Where f_2 = forward rate, r_1 = interest rate for the 1 year, r_2 = interest rate for the 2 year

Finance 1 – IBEB – Lecture 3 & Exercise lecture 3, week 3

Investment decision rules

1. Net present value (NPV)

$$NPV = \sum_{t=0}^T \frac{CF_t}{(1 + R_t)^t} = -INV_0 + \sum_{t=0}^T \frac{CF_t}{(1 + R_t)^t}$$

- Where INV, is the initial investment

The NPV measures economic value creation, so $NPV > 0$ is attractive, we choose the investment with the highest NPV

Complexities in Using NPV

1. Comparing projects with varying durations.
2. Capital constraints

Duration of the projects

For ongoing projects, a fair comparison of NPV can only be done when periods are equal, for example:

- Project A: Invest 50 today to earn 80 per year in the next three years
- Project B: Invest 50 today to earn 100 per year in the next two years

First, we need to extend the projects until the duration is equal, **then** we calculate the NPV of both in the extended form

Project A:

	T=0	1	2	3	4	5	6
A CF	-50	80	80	80			
A2 CF				-50	80	80	80

Project B:

	T=0	1	2	3	4	5	6
B CF	-50	100	100				
B2 CF			-50	100	100		
B3 CF					-50	100	100

As you can see we have extended the duration to 6 years by repeating the investment, doing so gives the following NPV

- A + A2: NPV of 261mln €

- B + B2 + B3: NPV of 310mln €

So, we choose Project B, unlike without adjusting for time we would have chosen A

Capital constraints

Sometimes firms have many positive NPV projects and they can't invest in all of them simultaneously

To tackle this, we take the following steps:

Step 1: Form all possible combinations between available projects

Step 2: Cancel those combinations that are impossible due to limited budget

Step 3: Choose the combination with the highest NPV

We have projects A, B & C each costing 100, but we only have 200€, and **no negative cash flow is allowed for t = 1 and t = 2**

	A	B	C	A&B	A&C	B&C	A&B&C	Nothing
t = 0	-100.0	-100.0	-100.0	-200.0	-200.0	-200.0	-300.0	0.0
t = 1	109.0	0.0	-105.0	109.0	4.0	-105.0	4.0	0.0
t = 2	2.0	123.0	400.0	125.0	402.0	523.0	525.0	0.0
NPV (@10%)	0.7	1.7	135.1	2.4	135.9	136.8	137.5	0.0

- In this case we see that it is best to do A&C combined

The example above is a simple one with only 3 project which can be done manually, but when we have many projects and constraints, lots of computing power is needed to solve the problem

- We have simple heuristics that could work, profitability index

Profitability index (NPV per constrained resource) = NPV / Investments

It can be used to identify the optimal combination of projects to invest in under the budget constraint. Rank projects by PI and select the ones with the highest indicator.

$$PI = \frac{\text{value created}}{\text{resource consumed}} = \frac{NPV}{\text{resource consumed}}$$

Note: It needs to meet 2 important constraints

- Set of projects taken following the PI ranking should completely exhaust the available resources
- There is only a single relevant resource constraint

Strengths of using NPV

- Often right and unambiguous
- Incorporates time value of money
- Easy to compare between projects
- Takes investment size into account
- Can compare one large project versus several smaller ones

Weakness:

- Needs an appropriate discount rate

The **correct methods** for the right investment decision are the ones we talked about above, alternative methods may be more practical in some circumstances, but may be wrong

2. Payback period

The payback period (PBP): The amount of time it takes to recover or pay back the initial investment

A firm must invest £150M to set up a factory that will sell products forever, earning £10M annually. The interest rate is 7%

- Payback period = $150/10 = 15$ years

Criteria to invest depends on what is set by the firm

- **Invest**, if payback period < required payback (set by the firm)
- **Do not invest** if payback period > required payback, e.g. when required payback = 10 years
- Choose the one with shortest payback period when there is options
- The formula below tell us that the payback period is the first moment when total cash inflows become **greater than or equal to** the initial investment

$$INV_{t=0} \leq \sum_{t=1}^{PBP} CF_t$$

Pitfalls of the PBP method

- It ignores cash flows after the payback period
- It ignores time value of money

3. Internal rate of return (IRR)

Internal rate of return (IRR) is the interest rate at which the NPV of an investment project equals zero.

A firm must invest £150M to set up a factory that will sell products forever, earning £10M annually. The interest rate is 7%

- The NPV is equal to 0 when, $(10 / \text{IRR}) - 150 = 0$
- $\text{IRR} = 6.6\%$

Criteria for investing

- Invest, if $\text{IRR} > \text{cost of capital}$ (if the IRR is larger than the true discount rate)
- Do not invest, if $\text{IRR} < \text{cost of capital}$

When choosing among several projects, choose the one with the **highest IRR**. But firms have good reasons not to base their decision on the highest IRR, due to the following reasons

- It ignores the size of a project, and with longer duration projects where reinvestment is assumed this might be a disadvantage.
- In case of positive and negative cash flows there is a possibility for multiple IRRs to exist with positive and negative interest rates when NPV is zero.

In the example below you can see the calculations with all 3 methods

- For Project A we see that using the PBP it shows that it only requires 1 year, but actually the NPV shows that it's negative, this is because **PBP ignores cash flows after the payback period, in this case it was negative**
- For Projects B & C, we see that their IRR are very similar but their NPV are vastly different, this is because **IRR ignores scale**, meaning it's only a ratio without capturing the size

Project	t = 0	t = 1	t = 2	t = 3	t = 4
A	-10	10.5	0	0	0
B	-100	0	0	0	300
C	-10	0	0	0	31

PBP	IRR	NPV (@10%)
1	5.0%	-0.45
4	31.6%	104.90
4	32.7%	11.17

Capital budgeting

When we decide to invest in a project, we want to know how our total cash flows change because of that project

- For that we need incremental earnings, which is different from total earnings

Capital budgeting is about:

- Forecasting free cash flows
- Understanding incremental earnings
- Dealing with uncertainty

Using the formulas below it is easy to calculate the FCF for historical data, the difficult part and what analysts spend most of their time on is forecasting

$$\text{net working capital} = \text{current assets} - \text{current liabilities}$$

$$\text{Free Cash Flow} = (\text{Revenues} - \text{Costs} - \text{Depreciation}) \times (1 - \tau) + \text{Depreciation} - \Delta\text{NWC} - \text{CapEx}$$

Incremental cash flows = the difference between doing and not doing the project.

Cannibalization occurs when the introduction of a new product has an adverse impact on the sales of existing products.

Opportunity cost - the revenue that could have been earned with an alternative use of the asset

- Think of machines that you own but are currently **idle**, you start a new project and use them, but this is not free, there is an opportunity cost, like selling the machines, these are earnings that we won't receive if we use it for the project
- Remember we care about **incremental earnings**, not doing the project gives you cash flow from selling the machine, so this is a cost

Sunk costs - unrecoverable costs that are already incurred and therefore irrelevant for the decision making.

Dealing with uncertainty

- **Break-even** analysis: this analysis finds the value of a parameter for which the $NPV = 0$. After this we can determine how likely it is that the parameter value is below or above the break-even amount
- **Sensitivity** analysis: input assumptions in this analysis will be changed within a plausible range, which will affect the NPV.
- **Scenario** analysis: in this analysis, the values of parameters will be determined for multiple scenarios, like a best case and worst case. These scenarios will be compared by their NPV when multiple parameters are changed at the same time.

Valuing stocks

For bonds, the cash flows were known, they consisted of coupons and a principal. But stock only pays dividends, we get the value of what is left of the earnings of a company, which are not known in advance.

Terminology

- Common Stock: security representing a share in the ownership of a corporation.
- Initial Public Offering: the first sale of stock in a corporation to the public.
- Secondary Market: a market, often a stock exchange, in which previously issued shares are traded amongst investors.
- Dividends: payments made by companies to shareholders.
- Dividend yield: ratio of annual dividend to share price. There are different types (for example, stock or cash; preferred and common)
- P/E Ratio: share price divided by earnings per share (price-to-earnings)

Two ways to estimate the value of a stock: **Dividend Discount Model (DDM)** or estimating the **value using comparable firms**.

Dividend Discount Model (DDM)

Price of today based on expected payments, dividends are also accounted for in the return

$$P_0 = \frac{div_1}{1 + r_E} + \frac{P_1}{1 + r_E} \Rightarrow r_E = \frac{div_1}{P_0} + \frac{P_1 - P_0}{P_0}$$

- where $\frac{div_1}{P_0}$ represents dividend yield,
- and $\frac{P_1 - P_0}{P_0}$ the capital gains rate.

Now since we know the formula for P_0 , we can replace every "price" with a future price

$$P_1 = \frac{div_2}{1 + r_E} + \frac{P_2}{1 + r_E}$$

$$P_0 = \frac{div_1}{1 + r_E} + \frac{div_2}{(1 + r_E)^2} + \frac{P_2}{(1 + r_E)^2}$$

Now if we keep on replacing with future prices we will be left with only the dividend part, this is because, same as for perpetuity as long as the growth is lower than r_E

$$P_0 = \sum_{i=1}^{\infty} \frac{div_{t+i}}{(1 + R_E)^i}$$

$$R_E = R_t + \text{equity risk premium}$$

The **Gordon (growth) model**

Zero dividend growth (i.e. constant dividend)

$$P_t = \frac{D}{r_e}$$

Constant dividend growth with factor g

$$P_t = \frac{D}{r_e - g}$$

Multiple valuation of comparable stocks

A company does not have to pay all earnings, they can keep them as retained earnings, which they can use for new investments.

$$div_t = \text{EarningsPerShare}_t \times \text{Dividend payout rate } (k)_t$$

Following the **Gordon growth model**

$$\text{Price}_{t=0} = \frac{\text{Dividend}_{t=1}}{Re - g} = \frac{k \cdot \text{EPS}}{Re - g}$$

By combining these formulas, we can arrive at P/E ratio:

$$\frac{Price_{t=0}}{Earnings} = \frac{k \cdot EPS}{Re - g} \cdot \frac{1}{EPS} = \frac{k}{Re - g}$$

Other multiples include:

- Earnings based: EV / EBIT(DA)
- Sales based: P / Sales or EV / Sales
- Asset-based: P / book value, EV / assets
- Cash flow based: P / cash flows
- Sector specific: Price / users, Price / subscribers, EV / capacity

Alternative models for price stocks

Total payout model

- $P_0 = PV(\text{Future total dividends and share repurchases}) / \text{shares outstanding}_0$

Discounted FCF model

$$P_0 = \frac{(V_0 + \text{cash}_0 - \text{debt}_0)}{\text{shares outstanding}_0}$$

- Where, $V_0 = PV(\text{FCF}'s)$

Theories

- Efficient market hypothesis: Based on available information, it is not possible to systematically achieve abnormal returns
- Informational efficiency: All relevant information is fully reflected in market prices
 - Price adjustments as a result of new information are direct and correct, **No over/under reaction**
 - Price = value, **No over or undervaluation**

Finance 1 – IBEB – Lecture 4 and Exercise lecture 4, week 4

Valuing stocks

Information

The first version of the three levels of informational efficiency was constructed by Fama in 1970:

- **Weak:** The stock prices reflect all information on its historical price. In technical analysis, trends of history are used to predict the future, but these cannot be considered useful.
- **Semi-strong:** the prices of the stock are based on the publicly available information which is relevant for pricing. The prices adjust to public information.
- **Strong:** not only is the publicly available information reflected in the prices, but also insider information of firms which is not yet public to all investors.

Lessons from efficient markets

Efficient market hypothesis - when relevant information is available it is immediately and completely reflected in prices, therefore it is not possible to systematically achieve abnormal profits.

- For investors to consistently beat the market, competitive advantage is needed, with low transaction costs, no regulation, no benchmark index, etc.
- Arbitrage opportunities are rare and short-lived
 - There are companies that use LLM to trade within milliseconds when new information is out e.g. High frequency trading

Two competing views

- Efficient markets (Fama): prices reflect information quickly
 - Abnormal returns hard to predict
- Behavioral Finance (Thaler): psychology and limits to arbitrage can create systematic mispricing

To determine whether a market is efficient, we need a theory for risk and return.

Measuring risk

Risk and return measures

Example

Stock has 3 possible returns: -10%, 5%, and 15% which happen with 1/3 probability

What is the expected return (μ), variance (σ^2) and standard deviation (σ)?

- Expected return: weighted average of returns

$$\left(-0.10 \cdot \frac{1}{3}\right) + \left(0.05 \cdot \frac{1}{3}\right) + \left(0.15 \cdot \frac{1}{3}\right) = 3.3\%$$

- Variance: Weighted average of squared deviations from the expected return

$$\sigma^2 = \frac{1}{3} \cdot (-0.1 - 0.033)^2 + \frac{1}{3} \cdot (0.05 - 0.033)^2 + \frac{1}{3} \cdot (0.15 - 0.033)^2 = 0.014$$

The standard deviation or volatility is $\sigma = 11.94\%$

Expected return, for a portfolio with N possible return and probabilities

$$E[R_p] = \sum_{i=1}^N P_i \cdot R_i$$

Variance - indicates how much the squared deviation from the mean is, which can be calculated with the formula:

$$\sigma^2 = \sum_{i=1}^N P_i (R_i - \bar{R})^2$$

The standard deviation, $\sigma(R)$, which is the square root of the variance, in Finance is also known as **volatility**.

Historical returns

The example and formulas used in the previous page is based on outcome probabilities which are 'expected', thus we consider them the population

Instead of using expected outcomes, historical data which are 'realized' can be used to estimate risk and return

- However, more historical data, means more different world

- The main difference is that with historical data we are working with a sample

Expected return, this formula stays the same as before

Variance, we are working with a sample and not a population

- Suppose we have K years of annual returns on a stock, meaning K N° of observations

$$s^2 = \frac{1}{K-1} \sum_{i=1}^K (R_i - \bar{R})^2$$

Example

What if I have 5 years of annual returns on say the S&P 500?

- Year 1: -35.6%, Year 2: 32.4%, Year 3: 16.5%, Year 4: 3.8%, Year 5: 13.8%.
- Average return: 6.2%

$$s^2 = \frac{1}{4} \cdot ((-0.356 - 0.062)^2 + (0.324 - 0.062)^2 + (0.165 - 0.062)^2 + (0.038 - 0.062)^2 + (0.138 - 0.062)^2)$$

$$s = \sqrt{0.065} = 25.5\%$$

Portfolio risk and return

What is a portfolio?

A portfolio is a collection of securities

- Every stock has it's own average risk and return
- To calculate the risk and return of the entire portfolio we need to factor in how these returns covary with each other

Main notations

- N is the number of assets in your portfolio
- x_i is the fraction of your wealth allocated to each asset i (1 to N)
- σ_i^2 is the variance of the return on asset i
- $p_{i,j}$ is the correlation between the returns on stocks i and j

Simple example

Say you have 10,000 euros allocated over 50 different companies

- You own 2 shares of ASML stock worth 1,150 euros per share

Portfolio weight is $\frac{2 \cdot 1150}{10000} = 23\%$

Portfolio average returns

Portfolio weights must sum to one: $\sum_i x_i = 1$

But they can be positive, zero or even negative!

- In the stock-market: short sales
- Selling an asset you do not own!
- Repurchase at a later date and deliver it to the lender
- Can be done typically by professional investors or market makers

But many 'retail' investors have credit or lend their assets

$$E(R_p) = \mu_1 \cdot x_1 + \mu_2 \cdot x_2 + \dots + \mu_N \cdot x_N$$

$$E(R_p) = \sum_{i=1}^N \mu_i x_i$$

Portfolio return variance

To calculate the variance of a portfolio $Var(R_p)$

- The variance of each asset i in the portfolio: σ_i^2
- The portfolio weight of each asset i : x_i
- The covariance of the return of each asset with other asset: $Cov(r_i, r_j) = \sigma_{i,j}$

You need to capture all these ingredients in one generalized formula, as we derive below for a two-asset case:

$$Var(R_p) = \sum_{i=1}^N \sum_{j=1}^N x_i x_j \sigma_{i,j}$$

This general formula for a two-asset case can also be written as:

$$Var(R_p) = x_1 x_1 \sigma_{1,1} + x_1 x_2 \sigma_{1,2} + x_2 x_1 \sigma_{2,1} + x_2 x_2 \sigma_{2,2}$$

- We know $\sigma_{1,1} = Cov(r_1, r_1) = Var(r_1) = \sigma_1^2$ and $\sigma_{2,2} = Cov(r_2, r_2) = Var(r_2) = \sigma_2^2$

$$Var(R_p) = x_1^2 \sigma_1^2 + x_1 x_2 \sigma_{1,2} + x_2 x_1 \sigma_{2,1} + x_2^2 \sigma_2^2$$

- We also know that $Cov(r_2, r_1) = Cov(r_1, r_2) = \sigma_{2,1} = \sigma_{1,2}$

- And $\sigma_{1,2} = \rho_{1,2} \sigma_1 \sigma_2$ **because** $\rho_{1,2} = \frac{Cov(r_1, r_2)}{\sigma_1 \sigma_2} = \frac{\sigma_{1,2}}{\sigma_1 \sigma_2}$

Final formula:

$$Var(R_p) = x_1^2 \sigma_1^2 + x_2^2 \sigma_2^2 + 2x_1 x_2 \rho_{1,2} \sigma_1 \sigma_2$$

Example

Consider two stocks with a correlation of 0.15

- Stock 1: Expected return 20%, standard deviation 30%, invested 100 million
- Stock 2: Expected return 12%, standard deviation 18%, invested 300 million

$$E(R_p) = 0.25 * 0.20 + 0.75 * 0.12 = 0.14 = 14\%$$

$$Var(R_p) = 0.25^2 * 0.30^2 + 0.75^2 * 0.18^2 + 2 * 0.25 * 0.75 * 0.15 * 0.30 * 0.18 = 0.0268$$

The portfolio standard deviation is 16.4%

- Lower than both individual assets, meaning lower risk

Diversification

Diversification in stock portfolios

The key theory that we follow to understand risk and return in portfolios is

'Markowitz (1952) portfolio theory', where we assume

- Investors like return
 - If 2 investments have the same risk, but one has a higher mean return then, investor will choose the one with higher mean return
- Investors dislike risk
 - If 2 investments have the same Mean return, but one has a higher risk (std dev) then, investor will choose the one with lower risk

Diversification eliminates **'idiosyncratic risk'**

- Idiosyncratic risk = stock/firm-specific risk
- The smaller correlation between stocks the more opportunities for risk reduction

Example

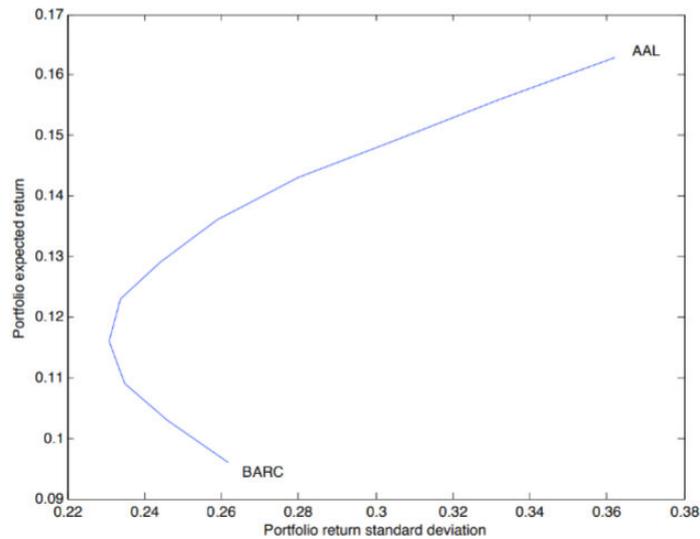
Suppose we have 2 stocks where correlation between their returns is 0.2

Stock	$E(R_i)$	σ_i
AAL	16.3%	36.2%
BARC	9.6%	26.2%

The following table shows what happens to the portfolio risk and return if we vary the weights

x_{AAL}	x_{BARC}	$E(R_i)$	σ_i
0	1	0.096	0.262
0.1	0.9	0.103	0.246
0.2	0.8	0.109	0.235
0.3	0.7	0.116	0.231
0.4	0.6	0.123	0.234
0.5	0.5	0.129	0.244
0.6	0.4	0.136	0.259
0.7	0.3	0.143	0.28
0.8	0.2	0.149	0.304
0.9	0.1	0.156	0.332
1	0	0.163	0.362

If we plot the Expected return and the return standard deviation, we get the '**Mean variance frontier**'

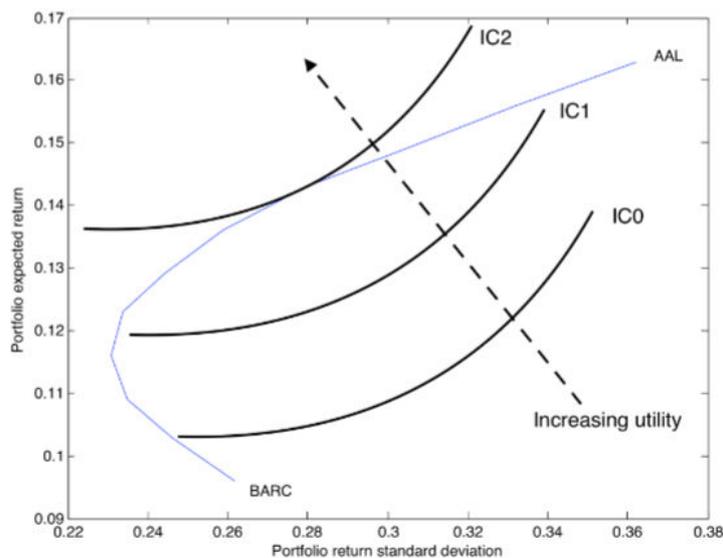


Note: one cannot infinitely reduce risk, this is because stock prices are not perfectly correlated with each other, meaning market-wide or 'systematic' risk shocks move all stocks to some degree

Optimal portfolio choice

From the mean variance frontier plot we can see all the possible combinations of portfolio risk and return, based on the weights, typically investors like return but dislike risk, so we assume '**risk aversion**'

- Thus, we can plot the indifference curves based on his risk aversion and get the optimal portfolio (point of tangency)
- **Note:** indifference curve varies across preferences



So far, we have assumed that all assets are risky, if we add a risk-free asset

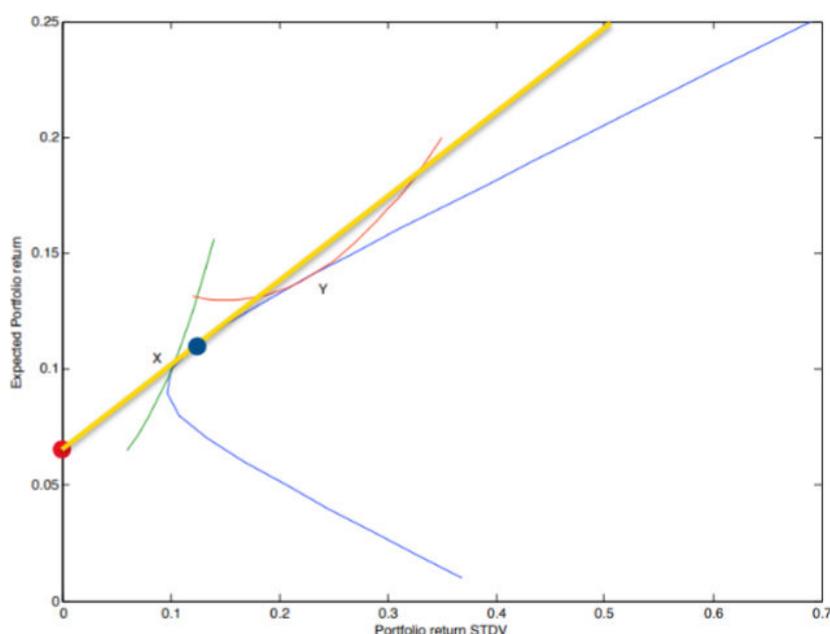
- Return known in advance
- No risk, so standard deviation is 0
- Return is uncorrelated to other assets that are not risk-free

In the graph below the

- Blue dot is the **tangency-portfolio** which tells us the optimal portfolio of risky assets (**Market portfolio**) that maximises return per unit of risk, based on the **Sharpe ratio**

$$\text{Sharpe ratio} = \frac{\text{Expected return} - \text{Risk free return}}{\text{Portfolio volatility}}$$

- Red dot represents the **risk-free asset**
- Yellow line is the **Capital market line**, which shows the highest possible combination of risk and return when you are allowed to combine risk-free assets and the market portfolio



Capital Asset Pricing Model (CAPM)

CAPM tells us how stocks should be priced if we believe in Markowitz theory, it starts with the assumption that everyone holds the market portfolio and the risk-free asset, with the only difference being the weights

- The **Firm specific risk** can be diversified away
- However, **Market risk** requires compensation, because it's 'systematic' risk that cannot be diversified away

- This is measured by β , the sensitivity of the investment I to the fluctuations of the Market portfolio

So, if the only risk that matter is the Market risk and this is measured by β , then β will price all the stocks, according to CAPM

The CAPM equation

$$E(R_i) = R_f + \beta_i(E(R_M) - R_f), \quad \beta_i = \frac{Cov(R_i, R_M)}{Var(R_M)}$$

- The risk-free rate R_f .
- The market risk premium: $(R_m - R_f)$
 - R_m is the market portfolio return
- β_i measures asset i 's risk.
 - Taking more risk, means requiring more compensation
 - Expected return is linearly increasing in risk.

Implications of β_i

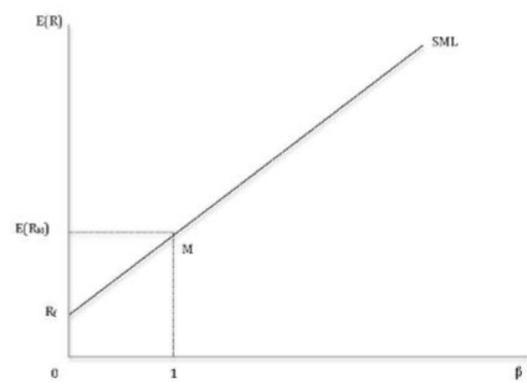
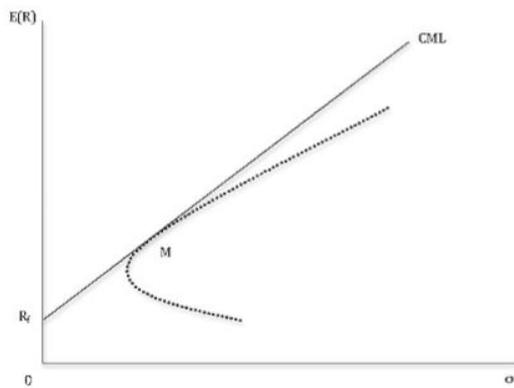
- A zero β asset carries no market risk: earns the risk-free rate (R_f)
- An asset with a β above one is said to be aggressive
 - Moves more than the market if the market moves
- An asset with a β between 0 and 1 is said to be defensive
 - Moves less than the market if the market moves
- Beta can also be negative
 - Rare

Capital market line & Security market line

The capital market line (CML) shows the highest possible combination of risk and return when you are allowed to combine risk-free assets and the market portfolio

- Where the only thing that varies is the weight between the market portfolio and the risk-free asset

The Security market line (SML), this is the plot of β versus expected return, according to CAPM all securities should lie on this line



Deviations from SML

The CAPM tells us the return that a stock should earn based on its risk, so if a stock is above the SML

- That stock has a higher expected return than the CAPM says it should have.
 - **Abnormal or excess positive return**
 - We call this deviation alpha, meaning the stock is currently under-priced.
- Trading implication: buy the stock and give it a higher weight (buy the stock)
- You earn expected return without bearing the appropriate level of risk

Finance 1 – IBEB – Lecture and Exercise lecture 5, week 5

Cost of capital

Resources are not obtained by a firm for free, because this amount could have been used to fund other projects. Thus, the opportunity cost of using this resource is equal to the value it would have when using the resource for the best possible alternative. The cost of capital of an investment is the expected return of available investments with the same beta.

- Debt cost of capital
- Equity cost of capital
- Project cost of capital

Equity cost of capital

The CAPM can be used to estimate cost of capital this estimate is provided by the Security Market Line (SML) equation:

$$r_i = r_f + \beta_i \times (E(R_{mkt}) - r_f)$$

The cost of capital of any investment opportunity equals the expected return of available investments with the same beta, to estimate the formula we need an estimate of:

- The risk free rate
- The expected return on the market
- The beta

The Market Portfolio

The market portfolio is almost impossible to define because there are just too many assets which are illiquid

- The S&P 500 is used the most as it's the most common with large amounts of data, but it only reflects about 10% of global wealth

- If you want to invest in the S&P 500 and hold it as the market portfolio, then in theory you should hold a value weighted portfolio of all stock that comprise the S&P 500

Value-Weighted Portfolio – a portfolio that consists of securities that are held in proportion to their market capitalization.

Additionally, it is also a **Passive portfolio** that does not require rebalancing even if market prices change.

In a portfolio like the market portfolio the investment in each security i is proportional to its market capitalization:

$$MV_i = (\text{Number of Shares of } i \text{ Outstanding}) \cdot (\text{Price of } i \text{ per share}) = N_i \cdot P_i$$

The weight of each security in the portfolio can be calculated as follows:

$$x_i = \frac{\text{Market Value of } i}{\text{Total Market Value of all securities}} = \frac{MV_i}{\sum_j MV_j}$$

The Market Risk Premium

We need to determine the risk-free rate

- The yield on US Treasury securities is most commonly used due to its liquidity
- Using mostly 10-to-30-year treasuries

The risk premium ($E(R_{mkt}) - r_f$) on the market can be estimated using the **historical** average excess return of the market over the risk-free interest rate however, there are **drawbacks** for using historical data.

- Standard errors of estimates are large, or data sampling issues, causing returns difficult to measure
- It is backward-looking and, hence, may not be representative of current expectations

A **possible alternative** could be to look at what is implied by the market and solve for the discount rate:

$$r_{mkt} = \frac{div_1}{P_0} + g = \text{Dividend yield} + \text{Expected dividend growth rate}$$

Beta estimation

Beta is the expected percent change in the excess return of the security for a 1% change in the excess return of the market portfolio

Linear regression can be applied to estimate the excess return on stock i (dependent variable) with market excess return (independent variable)

- Due to measurement error, beta's are easier to estimate for (industry) portfolios than individual returns

$$(R_i - r_f) = \alpha_i + \beta_i(R_{mkt} - r_f) + \varepsilon_i$$

Where α_i is the intercept term, $\beta_i(R_{mkt} - r_f)$ is the sensitivity of the stock to market risk and ε_i is the error term (zero on average)

Essentially, α_i is the measure of historical return on stock against the estimation of SML.

- Positive alpha means that historical return on stock was better than predicted by CAPM
- Negative alpha means that historical return was below SML.

Debt cost of capital

Debt betas are hard to estimate because many bonds trade infrequently

Yield to maturity is the IRR an investor will earn from holding the bond to maturity and receiving its promised payments.

- If there is little risk the firm will default, yield to maturity is a reasonable estimate of investors' expected rate of return.
- If there is significant risk of default, yield to maturity will overstate investors' expected return.

Consider a one-year bond with YTM of y

- For each \$1 invested in the bond today, the issuer promises to pay $\$(1 + y)$ in one year
- Suppose the bond will default with probability p , in which case bond holders receive only $\$(1 + y - L)$, where L is the expected loss per \$1 of debt in the event of default.

Expected return of the bonds can be calculated using the formula:

$$r_d = (1 - p)y + p(y - L) = y - pL$$

$$= \text{Yield to Maturity} - \text{probability of default} \times \text{Expected loss rate}$$

Example – using expected default rate

Consider a firm with a 4 year ‘junk’ bond with a CCC rating. The yield to maturity is 12%. The risk-free rate is 5% and the risk premium is 7%.

- We are not in a crisis
- Expected loss rate of 60%

Rating:	AAA	AA	A	BBB	BB	B	CCC	CC-C
Default Rate:								
Average	0.0%	0.1%	0.2%	0.5%	2.2%	5.5%	12.2%	14.1%
In Recessions	0.0%	1.0%	3.0%	3.0%	8.0%	16.0%	48.0%	79.0%

Compute the expected return on this debt, using the average historical default rates by rating from the table

- $y - pL$, where p is 12.2%
- $0.12 - (0.122 \cdot 0.6) = 4.68\%$

Example – using average betas

Consider a firm with a 4 year ‘junk’ bond with a CCC rating. The yield to maturity is 12%. The risk-free rate is 5% and the risk premium is 7%.

- Expected loss rate of 60%

Rating:	A or more	BBB	BB	B	CCC
Debt beta	<0.05	0.10	0.17	0.26	0.31

This time we apply the CAPM

- Risk-free + (beta · YTM)
- $0.05 + 0.31 \cdot 0.07 = 7.17\%$

Project’s cost of capital

All-equity comparables

To measure the compensation for the risk of a new project when it is fully equity financed, but different from the average project in the company, we want to find an all-equity financed firm with similar business operations to a new project for comparison.

By using comparable firm's beta and cost of capital we can estimate the cost of capital for the new project.

- If it is not possible to find an all-equity financed firm we can also make estimates from a levered firm (financed by both debt and equity) with similar business activities.
- As a result of having debt financing the return on equity will be higher due to higher risk. Hence we want to use the unlevered cost of capital.

The **unlevered cost of capital** - the expected return required by investors to hold the firm's underlying

The weighted average of the firm's equity and debt cost of capital can be calculated using the formula:

$$r_u = \frac{E}{E+D} \times r_E + \frac{D}{E+D} \times r_D$$

Note: "perfect" world without taxes and frictions assumed

Similarly: Unlevered Beta

$$\beta_u = \frac{E}{E+D} \times \beta_E + \frac{D}{E+D} \times \beta_D$$

When calculating $\frac{D}{E+D}$ ratio it is important to use the net debt. This is because cash is a risk-free asset that reduces the average risk of a firm's assets.

$$\text{Net Debt} = \text{Debt} - \text{Excess cash} - \text{Short term investments}$$

Operating Leverage is the proportion of fixed to variable costs of the project.

- A higher proportion of fixed costs implies higher sensitivity of the project's cash flows to market risks, meaning higher beta and cost of capital.

The Weighted Average Cost of Capital (WACC)

When the assumption of the "perfect" world is relaxed, we need to account for taxes.

$$\text{Effective after-tax interest rate} = r(1 - \tau_c)$$

The Weighted Average Cost of Capital is then equal to:

$$r_{WACC} = \frac{E}{E+D} \times r_E + \frac{D}{E+D} \times r_D \times (1 - \tau_c)$$

Given a target leverage ratio:

$$r_{WACC} = r_u - \frac{D}{E + D} \times \tau_c r_D$$

Where r_u is the unlevered cost of capital or pre-tax WACC.

WACC and pre-tax WACC

Unlevered cost of capital shows the expected return on holding a firm's assets, which in the real world with taxes can be used for evaluation of all-equity projects with the same risk as the firm.

- Taking into account taxes, WACC adjusts for the capital structure of the firm.

Investor behavior and capital efficiency

Competition and Capital markets

Stock's alpha - the difference between a stock's expected return and its required return according to the security market line (CAPM return). When the market portfolio is efficient all stocks are on SML and alpha is equal to zero.

Stock's alpha: $\alpha_s = E[R_s] - r_s$

Security market line: $r_s = r_f + \beta_s \times (E[R_{mkt}] - r_f)$

Deviation from SML

Stock prices adjust to news

- Positive alpha (=higher expected return than CAPM predicts)
- Investors buy at a lower price than CAPM prediction until expected returns go down again
- The stock is back on SML

Information and rational expectation

Informed Vs. Uninformed Investors

- In the CAPM framework, investors should hold the market portfolio combined with risk-free investments.
- An uninformed investor can buy an ETF and T-bills

- Provides an alpha of zero (if market is efficient)
- Prices should respond to information

The market portfolio can be inefficient if

- Information was misinterpreted by a substantial number of investors who believe they are earning a positive alpha when they are actually earning a negative alpha
- A significant number of investors are willingly hold inefficient portfolio because they also care about other aspects of portfolios other than returns and volatility (like ESG)

Systematic trading biases

Biases become problematic when they occur systematically instead of randomly. Some common biases are:

- **Disposition effect**- tendency to hold losing stocks for too long, as investors do not want to realize losses
- **Herd behavior**- occurs when individuals start actively following each other

Multiple factor model

CAPM used so far is an example of a **single-factor model** which assumes that the only risk is market risk, however there is a debate whether markets are truly efficient.

3 main patterns have been observed which is debated on whether they are just temporary or actually persistent

- Small market capitalization stocks have historically earned higher average returns than the market portfolio, even after accounting for their higher beta. **"Small Cap" stocks**
- High book-to-market stocks have historically earned higher average returns than low book-to-market stocks. **"Value" stocks**
- Buy stocks with high-past returns and short stocks with past low returns.

Momentum

Multi-factor model of risk is used where there are other factors that explain returns, hence, CAPM proposed portfolios may not be efficient. In this case, to

construct efficient portfolios we need to use factor portfolios that are covering different risk factors.

Multifactor model of risk for given N factor portfolios:

$$E[R_S] = r_f + \beta_S^{F1} \times (E[R_{F1}] - r_f) + \beta_S^{F2} \times (E[R_{F2}] - r_f) + \dots + \beta_S^{FN} \times (E[R_{FN}] - r_f) = r_f + \sum_{n=1}^N \beta_S^{FN} \times (E[R_{FN}] - r_f)$$

The **Arbitrage Pricing Theory (APT)** is an example of a multifactor model

Self-financing portfolio

A **self-financing portfolio** can be constructed by going short in some stocks and long in others with the same market value.

For self-financing factor portfolios the formula comes down to (as the risk free rate drops out):

$$E[R_S] = r_f + \beta_S^{F1} \times E[R_{F1}] + \beta_S^{F2} \times E[R_{F2}] + \dots + \beta_S^{FN} \times E[R_{FN}] = r_f + \sum_{n=1}^N \beta_S^{FN} \times (E[R_{FN}])$$

The Fama-French-Carhart (FFC) Factor Specifications was created to try and predict stock returns better than CAPM by incorporating other risks by creating a self-financing portfolio based on patterns we noted

- Buy small-cap stocks, short large cap stocks: **small-minus-big portfolio (SMB)**
- Buy high book-to-market (value) stocks, short low book-to-market stocks (growth): **high-minus-low portfolio (HML)**
- Buy stocks with high one-year past returns, short stocks with low past returns: **prior one-year momentum portfolio (PRIYR)**

$$E[R_S] = r_f + \beta_S^{Mkt} \times (E[R_{Mkt}] - r_f) + \beta_S^{SMB} \times (E[R_{SMB}] - r_f) + \beta_S^{HML} \times (E[R_{HML}] - r_f) + \beta_S^{PRIYR} \times (E[R_{PRIYR}] - r_f)$$

Finance 1 – IBEB – Lecture and Exercise lecture 6, week 6

Overview

In this lecture we mainly discuss the capital structure of a firm, meaning the relative proportion of debt, equity and other securities a firm has outstanding

- We will see how to finance a firm, whether to use debt or equity and in which proportions
- We shall do this first in a perfect and ideal world with no friction
- Then we will add more realistic components (taxes, distress costs) to see how it changes
- Finally, we will see how capital structure can incentivise managers

Modigliani-Miller without taxes

Suppose you decide to start a project, it requires 0.9 mil of upfront cost, and the pay-off is 0.9 mil when demand is low, and 1.3 mil when demand is high, with both a 50% chance

- Suppose risk premium demanded is 8%, risk-free rate is 2% and cost of capital is 10%

$$\text{Expected cash flow} = \frac{1}{2}(0.9\text{mil} + 1.3\text{mil}) = 1.1\text{mil}$$

$$\text{NPV} = -0.9 + \frac{1.1}{1.1} = 0.1\text{mil}$$

The project requires 900k upfront cost, but the PV of the discounted capital flows is 1mil, meaning the whole project is worth 1mil today, so

- We will raise 1mil in capital
- Where 100k is the profit for the entrepreneur

We have 2 options to fund this 1mil:

- Option 1: Fund 1m with equity: 10% cost of capital
- Option 2 Fund 500k with debt, 500k with equity
 - Borrow at 2% risk-free rate, so pay back 510k
 - Equity holders get either 900k – 510k = 390k (-22%) or 1300k – 510k = 790k (+58%)
 - So Expected equity return $0.5 \cdot (-22\% + 58\%) = 18\%$, debt return = 2%

As you can tell the cost of capital for both options are the same

- Option 1, unlevered equity: 10%
- Option 2, levered equity: $0.5 \cdot (2\% + 18\%) = 10\%$

This gave rise to the **Modigliani-Miller (MM) Proposition 1**, in a **perfect capital market**, the total value of a firm is equal to the market value of the total cash flows generated by its assets and is not affected by its choice of capital structure, following the **Law of One Price**

- Change in capital structure just **change how you distribute** the cash flows, not the cash flows themselves
 - The more debt you take on, the more risky the equity becomes, so the higher the levered equity cost of capital
 - The higher equity cost of capital will be offset by the low debt cost of capital

In the MM proposition we situate ourselves in a **perfect capital market**, and this means **assumptions** that could be very different from the real world

- Investors and firms can trade the same set of securities at competitive market prices equal to the present value of their future cash flows
- No taxes, transaction costs, or issuance costs associated with security trading
- A firm's financing decision do not change the cash flow generated by its investment nor do they reveal new information about them

Relating to MM proposition 1 is the concept of **homemade leverage**: If a firm does not take on debt (fully equity funded) but the investors want to earn a more risky and higher levered return, they can create their own leverage by borrowing money themselves to invest => **Return is the same as the levered equity return.**

Notation:

- E- market value of equity in a levered firm
- D- market value of debt in a levered firm
- U- market value of equity in an unlevered firm
- A- market value of firm's assets

MM Proposition I: In the presence of a perfect capital market, the market value of a firm is equal to the market value of its assets, and this cannot be affected by the chosen capital structure of the firm

$$E + D = U = A$$

So the returns must also follow this definition, thus we can say that the return on unlevered equity (R_U) is related to the returns of levered equity (R_E) and debt (R_D)

$$R_u = \frac{E}{E + D} \times R_E + \frac{D}{E + D} \times R_D$$

Solving for R_E :

$$R_E = R_u + \frac{D}{E}(R_u - R_D)$$

MM Proposition II: the cost of capital of levered equity is equal to the cost of capital for unlevered equity plus an additional risk premium due to leverage, that is proportional to the firm's market value debt-to-equity ratio.

- If you take on more debt/leverage the risk of the firm's equity increases, the risk of the firm's assets stays the same, so higher return required for the equity

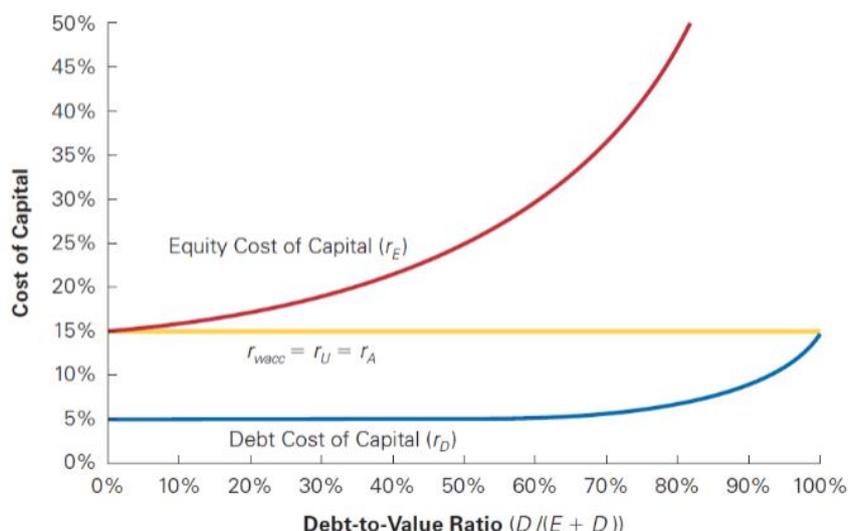
Connecting to the WACC we saw last lecture

- If a firm is levered, project r_A is equal to the firm's **weighted average cost of capital (WACC)**
- The Cost of capital (Pretax WACC) is independent of capital structure in perfect markets, and equal to the unlevered equity cost of capital

$$r_{wacc} = \left(\frac{\text{Fraction of Firm Value}}{\text{Financed by Equity}} \right) \left(\text{Equity Cost of Capital} \right) + \left(\frac{\text{Fraction of Firm Value}}{\text{Financed by Debt}} \right) \left(\text{Debt Cost of Capital} \right)$$

$$= \frac{E}{E + D} r_E + \frac{D}{E + D} r_D$$

$$r_{wacc} = r_U = r_A$$



As you can see the r_{wacc} stays constant for all levels of debt to value ratio, this is because as we saw in the simple example, increase in debt is exactly offset by an increase in the equity cost of capital

Beta: Similarly, the effect of leverage on the risk of security can be expressed in terms of beta: $\beta_E = \beta_u + \frac{D}{E}(\beta_u - \beta_D)$

Equity Issuances

Dilution- an increase in the total number of shares that will divide a fixed amount of earnings.

If a firm issues new shares, there will be no gain or loss for the shareholders if the shares are sold at a fair price.

- This is because the price of the share has to remain constant.
- But we do have **earnings dilution** in this case, this is because the same amount of earnings now has to be divided among more shares.
- Which leads us to the **dilution fallacy**, that if a firm starts issuing equity, this will reduce the value of the existing shares of the shareholders.
- But here it is not taken into account that if a firm starts issuing new shares, the cash earned by a firm will increase, thus a firm will have more assets and higher cash flows.

The increases of this will be equal to the dilution of the shares. The fallacy should not affect the decision on equity vs debt financing.

Conservation of Value Principle for Financial Markets

- With perfect capital markets, financial transactions **neither add nor destroy value**, but instead represent a repackaging of risk (and therefore return).
- This implies that any financial transaction that appears to be a good deal may be exploiting some type of market imperfection.

Capital structure with corporate tax

Now we move away from the perfect capital market and introduce **taxes**

- Corporations pay taxes on their profits after interest payments are deducted
- Thus, interest expense reduces the amount of corporate taxes
- This creates an incentive to use debt

Interest tax shield is the reduction in taxes paid due to the tax deductibility of interest

$$\text{Interest Tax Shield} = \text{Corporate Tax Rate} \times \text{Interest payments}$$

Meaning the cash flows a levered firm pays to investors will be higher than what they would be without leverage by the amount of the interest tax shield

$$\left(\begin{array}{c} \text{Cash Flows to Investors} \\ \text{with Leverage} \end{array} \right) = \left(\begin{array}{c} \text{Cash Flows to Investors} \\ \text{without Leverage} \end{array} \right) + (\text{Interest Tax Shield})$$

Example

	With Leverage	Without Leverage
EBIT	\$2800	\$2800
Interest expense	-400	0
Income before tax	2400	2800
Taxes (35%)	-840	-980
Net income	\$1560	\$1820

Tax savings of 35% * \$400mil = \$140mil

Modigliani-Miller with taxes

Proposition I: the value of firms with leverage will be higher than that without leverage due to tax savings from the debt.

$$V^L = V^U + PV(\text{Interest Tax Shield})$$

The present value of the tax shield depends on the **interest payments and the maturity of the debt** (affects future cash flows), and **earnings and tax rate risk** (affects discount rate), we have to assume

- Debt (D) is kept permanently, perpetuity
- Debt is riskless, so borrowed at the risk-free rate
- Tax rate (τ_c) are certain
- EBIT > Interest payments

So, interest tax shield each year is $\tau_c \cdot r_f \cdot D$, and tax shield can be valued as a perpetuity

$$\begin{aligned} PV(\text{Interest Tax Shield}) &= \frac{\tau_c \times \text{Interest}}{r_f} = \frac{\tau_c \times (r_f \times D)}{r_f} \\ &= \tau_c \times D \end{aligned}$$

Another way to derive PV(Interest tax shield)

- If debt is fairly priced, no arbitrage implies that it's market value = PV of all future interest payments

$$\text{Market Value of Debt} = D = PV(\text{Future Interest Payments})$$

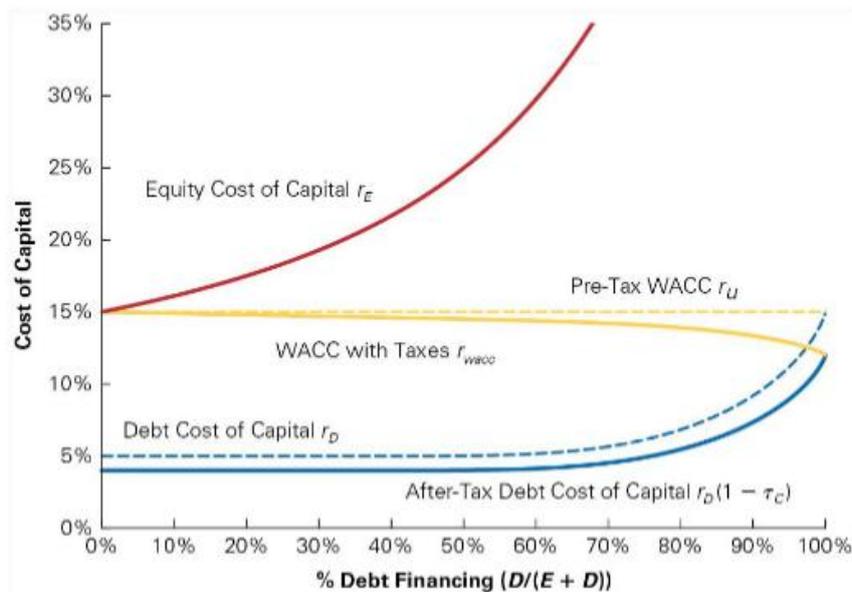
- If firm's marginal tax rate is constant

$$\begin{aligned}
PV(\text{Interest Tax Shield}) &= PV(\tau_c \times \text{Future Interest Payments}) \\
&= \tau_c \times PV(\text{Future Interest Payments}) \\
&= \tau_c \times D
\end{aligned}$$

Adjusting WACC

The weighted average cost of capital (WACC) (including taxes) will give us the effective after-tax cost of capital to the firm, where the reduction of the interest tax shield is taken into account.

$$r_{WACC} = \frac{E}{E + D} \times r_E + \frac{D}{E + D} \times r_D \times (1 - \tau_c)$$



Note: The debt Cost of Capital now becomes $r_D(1 - \tau_c)$

If corporate taxes are the only friction in the perfect world, it's optimal for firms to fully finance themselves with debt

- This maximises interest payments, so it maximises the PV of the tax shield
- Because of the tax reduction due to debt, the earnings are higher

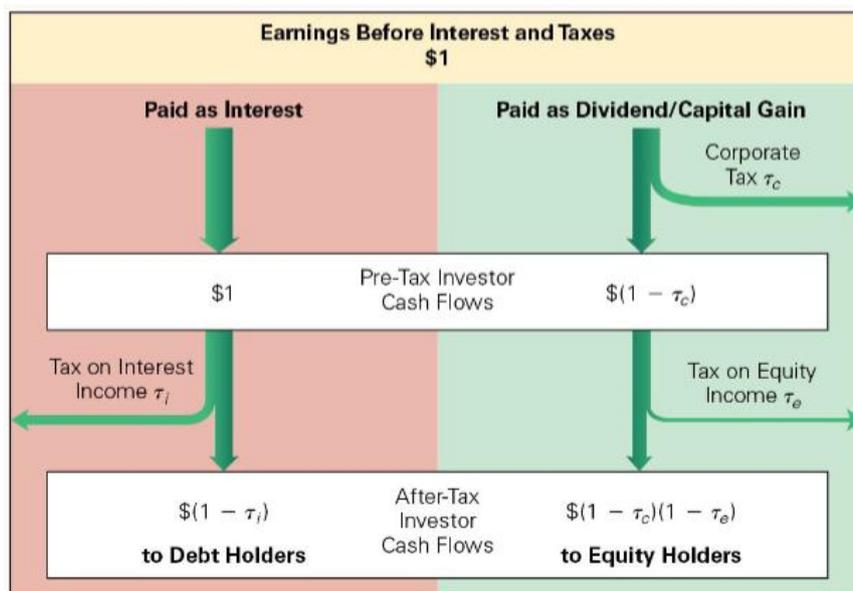
Capital structure with corporate tax and personal taxes

In the real world we not only have corporate tax, but also taxes on individuals, the amount of money they receive will depend on the cash flows after all taxes have been paid

- Interest payments from debt are taxed as income (typically)
- Equity investors must pay taxes on dividends and capital gains

Notation:

- τ_c - corporate tax rate,
- τ_i - personal tax rate on interest payments (debt income),
- τ_e - personal tax rate on dividends and capital gains (income from equity)



Now we assume that individuals also pay taxes, The **effective tax advantage of debt** (with personal tax) can be computed as follows:

$$\tau^* = \frac{(1 - \tau_i) - (1 - \tau_c)(1 - \tau_e)}{(1 - \tau_i)} = 1 - \frac{(1 - \tau_c)(1 - \tau_e)}{(1 - \tau_i)}$$

- In general, every \$1 received after taxes by debt holders from interest payments cost equity holders $\$(1 - \tau^*)$ on an after-tax basis

Now that we have included taxation on individuals and permanent debt, the value of the firm with leverage becomes

$$V^L = V^U + \tau^*D$$

- Usually, the Benefit of leverage is reduced in the presence of personal taxes, meaning $\tau^* < \tau_c$

With personal taxes, the **firm's equity and debt cost of capital will adjust** to compensate investors for their tax burdens, therefore, WACC will be calculated using the **same formula** as before:

$$r_{WACC} = \frac{E}{E+D} \times r_E + \frac{D}{E+D} \times r_D \times (1 - \tau_c)$$

Our model vs. reality

Our treatment of taxes is highly simplistic, and in reality much more complicated varying across individuals, firms and countries

- Firm differences: (firms with EBIT ≤ 0 can't pay interest)
- Tax codes are highly complicated
- Distress costs

The key lesson is that tax rates can have a significant impact on firm value and on capital structure decisions

- This makes taxes also a political instrument
- Cross-country differences in taxes make some countries more attractive for companies than others

Financial distress, managerial incentives & information

Financial distress: When a firm has trouble with paying the debt obligations that are due as a result of unstable cash flows.

Default: when a firm fails to make the required interest or principal payments on its debt or violates a debt covenant

- After the firm defaults, debt holders are given certain rights to the assets of the firm and may even take legal ownership of the firm's assets through bankruptcy

Leverage increases the risk of bankruptcy as debt is a formal commitment to pay the debt holder, whereas in **equity financing** a firm is not obligated to pay dividends.

If a firm has access to capital markets and can issue new securities at a fair price, **then it need not default as long as the market value of its assets exceeds its liabilities**

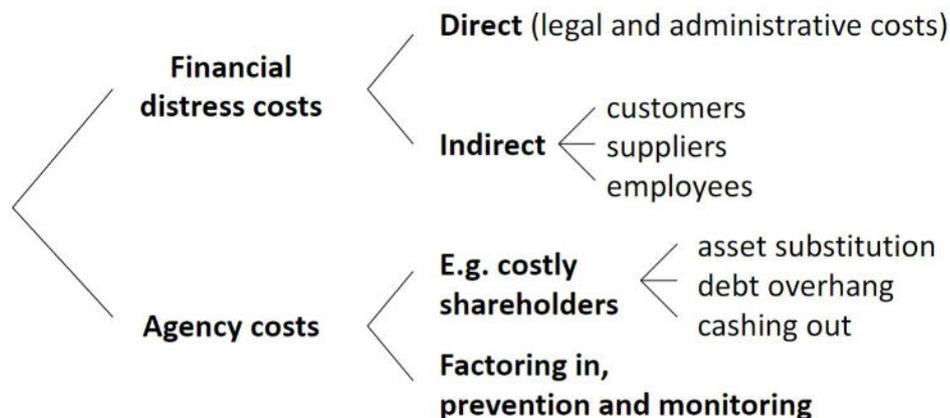
- If a firm does not have cash immediately available, it can raise the cash by obtaining a new loan or by issuing new shares
- Many firms experience years of negative cash flows yet remain solvent.
- Amazon made no profit for the first 7 years

If we have perfect capital markets, according to **MM proposition 1**, where total value of all investors does not depend on the firm's capital structure

- This means that there are **no costs to bankruptcy**, no disadvantage to debt financing, and a firm will have the same total value and will be able to raise the same amount initially from investors with either choice of capital structure

However, in the real world, **bankruptcy leads** to complicated process with **large economic costs**, as illustrated by the diagram below

- Given the direct costs of bankruptcy, firms may avoid filing for bankruptcy by first negotiating directly with creditors and reorganizing
- Full liquidation is costly and less common



If a new investment of a company fails and debt exceeds the market value of all assets, **equity holders** will lose their entire investment in the firm and will **not care about bankruptcy costs**

However, debt holders do care about these bankruptcy costs

- So, when they lend out they will pay less for the debt initially (PV of the bankruptcy cost less) or they will ask for a higher interest rate
- This reduces the firm value due higher interest rate thus, shareholders get less
- Meaning bankruptcy costs will be borne by the shareholders
- Thus: when securities are fairly priced, **shareholders pay the present value of the costs associated with bankruptcy and financial distress**

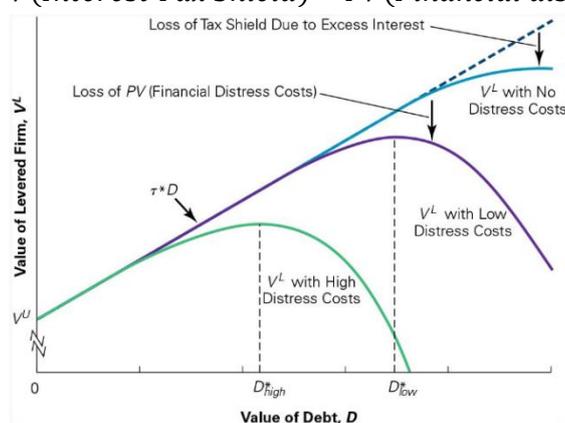
Tradeoff theory

Tradeoff Theory: the firm picks its capital structure by trading off the benefits of the tax shield from debt against the costs of financial distress and agency costs

Therefore, the total value of a levered firm is equal to the value of unlevered firm plus the present value of interest tax shield minus the present value of financial distress costs.

- The present value of financial distress costs is determined by, the probability of financial distress, their amount and the discount rate of distress costs

$$V^L = V^U + PV(\text{Interest Tax Shield}) - PV(\text{Financial distress costs})$$



As shown by the graph, the higher the distress costs, the lower the value of the levered firm and its debt, and the lower the distress costs, the higher the firm and debt value.

Agency costs

Agency costs are costs that are incurred when there are different interests between the holders of a firm. The costs will be created due to the conflicts between debt and equity holders that need to be solved due to the amount of leverage a firm chooses.

Excessive risk-taking

When a firm is in financial distress it may choose to engage in very risky activities with a small probability of large gains. In a firm, shareholders will be the owners of a firm, but they bet on risk with the money of the debt holders, which is known as **risk shifting**. Due to this, shareholders will take more risky assets instead of low-risk ones, for example by implementing a project with negative NPV, which is known as the **asset substitution problem**.

Under-investment

When a firm is in financial distress it may also choose not to invest in a new low-risk and NPV-positive project. Because part of the project gains will go to debt holders to resolve the financial distress, NPV to equity holders will be reduced and may even be negative, thus the shareholders would decline the project. The agency cost of debt reflected is the **debt overhang**.

Agency costs and the value of leverage

Leverage can encourage managers and shareholders to act in ways that reduce firm value.

- It appears that the equity holders benefit at the expense of the debt holders.
- However, ultimately, it is the shareholders of the firm who bear these agency costs.

These agency costs are priced in when new debt is issued. However, if a firm issues new debt, existing debtholders will bear part of the consequences.

- Example: if a firm is more likely to default due to new debt, part of the financial distress costs will be paid by existing debtholders

Leverage ratchet effect

Leverage ratchet effect: companies find it easier to increase leverage but much harder to reduce it.

When an unlevered firm issues new debt, equity holders bear any anticipated agency or bankruptcy cost through a discount in price they receive for that new debt. However, once a firm has debt already in place some of the agency or bankruptcy cost of taking additional leverage fall on existing debt holders.

1. Shareholders may have an incentive to increase leverage even when this does decrease the value of the firm.
2. Or the shareholders will not decrease leverage by buying back, even though this would increase the firm value.

If a firm would start issuing more debt, the r_D will increase, wealth will be transferred from debt holders to equity holders. Even though the firm value is reduced by increasing leverage, it does benefit shareholders.

Debt maturity and debt Covenants

To mitigate agency costs of debt, debt holders can either issue shorter term debt or use restrictions such as **debt covenants** (limit the firm's ability to pay large dividends, the types of investment the firm can make and the amount of new debt the firm can take on)

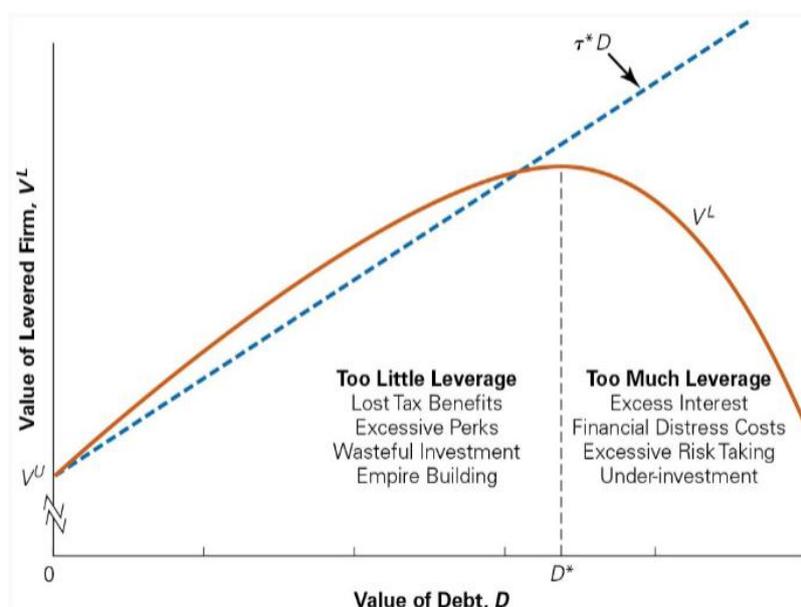
Optimal leverage with Taxes, Financial distress and Agency costs

For the optimal level of debt there will be a trade-off between the tax shield of debt against the costs of financial distress and agency costs, which is known as the trade-off theory

$$V^L = V^U + PV(\text{Interest Tax Shield}) - PV(\text{Financial distress costs}) - PV(\text{Agency cost of debt}) + PV(\text{Agency benefits of debt})$$

Agency benefits

- Maintain ownership concentration (equity stake)
- Reduce wasteful spending, which is more likely to when firms have excess cash (free cash flow hypothesis problem)
- Increase commitment (managers use more effective strategies when there's threat of financial distress)



The optimal debt level

R&D intensive firms: Firms with high R&D expenditures and low current free cash flow. Because of a low EBIT the tax shield needed is very small thus there is only a little bit of debt.

Mature firms: usually have stable cash flows, tangible assets and fewer investment opportunities. Because tangible assets will have a high liquidation

value, the financial distress costs will be low. The optimal level of debt for mature firms will be higher than that of growing firms

Information

Asymmetric Information

- A situation in which parties have different information.
- For example, when managers have superior information to investors regarding the firm's future cash flows.
- Investors can 'signal'
- Engage in acts that give credibility to the management's belief in success

Signaling Theory of Debt

- Use leverage to signal information
- If distress is costly to the firm, but the firm has private information that it thinks this will be unlikely, it can show this by taking on leverage

Pecking-Order theory

Similarly to trade-off theory, **Pecking-Order theory** explains the choice capital structure of a firm. In this case, the key assumption is asymmetric information, meaning the management of the company is informed better about the prospects, risks and future profitability of the company than outside capital providers. Because of that, capital providers tend to ask for a higher premium to compensate for information asymmetry.

The signaling effect then causes the pecking order of financing, in which the firm will **use the cheapest form of financing first**. In this theory, using retained earnings is the cheapest way of financing with a lowest degree of asymmetric information, whereas issuing new shares (new equity) is considered the most expensive and used only if other sources are already exhausted.

Internal financing → New debt → New equity

Issuing equity

A seller can give some information via the way he is selling his product. Because the bigger his desire to sell, the higher the probability the product is of low quality.

Adverse selection is when buyers and sellers have different information about the product. The **Lemons principle** states that when sellers have private information about the product and its value, buyers are likely to ask for lower prices because they do not know of which quality the product will be.

The Lemons principle implies that firms who start issuing new equity will sell these stocks at a discounted price to investors because investors are not willing to pay this much due to the possibility that bad news will be announced.

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